Discrete Math Days 2022 (DMD 20/22) Santander, 4–6 July 2022



Programme





Monday, July 4

Time	Aula 1	Aula 2	
8:15-8:50	Registration (Aula 6)		
9:00-9:25	Opening (Aula Magna)		
9:30-10:30	Pascal Schweitzer (Aula Magna) Chair: Marc Noy		
	Symmetry in discrete structures: graphs,	, groups and algorithms	
10:30-11:15	Coffee l	oreak	
	Chair: Juanjo Rué	Chair: Arnau Padrol	
11:15-11:35	Aida Abiad, Boris Brimkov, Sakander	Giulia Codenotti, Thomas Hall and Jo-	
	Hayat, Antonina P. Khramova and	hannes Hofscheier	
	Jack H. Koolen	Generalised flatness constants: a frame-	
	Extending a conjecture of Graham and	work applied in dimension 2	
	Lovász on the distance characteristic poly- nomial		
11:35-11:55	José Aliste-Prieto, Anna De Mier , Rosa	Eduardo Lucas Marín	
	Orellana and José Zamora	On discrete Borell-Brascamp-Lieb type in-	
	Polynomials for marked graphs and the	equalities for big negative parameters	
	chromatic symmetric function		
11:55-12:15	Olaf Parczyk, Sebastian Pokutta,	Bojan Bašić and Anna Slivková	
	Christoph Spiegel and Tibor Szabó	On the Heesch number in \mathbb{E}^d	
	New Ramsey Multiplicity Bounds and		
	Search Heuristics		
	<u>Chair: Öznur Yasar Diner</u>	<u>Chair: Julian Pfeifle</u>	
12:20-12:40	Delia Garijo, Andrew Goodall and Lluís	Davide Bolognini, Antonio Macchia, Gi-	
	Vena	ancarlo Rinaldo and Francesco Strazzanti	
	Homomorphisms between graphs embedded	Accessible set systems and a conjecture on	
12:40-13:00	<i>in surfaces</i> Irene Gil Fernández and Hong Liu	Cohen-Macaulay binomial edge ideals	
12:40-13:00	How to build a pillar: a proof of	Giulia Codenotti, Stephan Gardoll and Thorsten Theobald	
	Thomassen's conjecture	Combinatorics and preservation of coni-	
	Thomassen's conjecture	cally stable polynomials	
13:00-13:20	Jacob Lahne, David Orden , Kather-	Manuel Radons and Josué Tonelli-Cueto	
	ine Phetxumphou and Marino Tejedor-	Generalized Perron roots and solvability of	
	Romero	the absolute value equation	
	Linking+SensoGraph: A new graph-based		
	method for sensory analysis		

Lunch break (self-arranged)

	Chair: Aida Abiad	<u>Chair: Leo Liberti</u>	
16:30-16:50	Fábio Botler, Phablo F.S. Moura and	Marie-Charlotte Brandenburg, Chris-	
	Tássio Naia	tian Haase and Ngoc Mai Tran	
	Seymour's second neighborhood conjecture	Competitive equilibrium always exists for	
	in arbitrary orientations of a random graph	combinatorial auctions with graphical pric-	
		ing schemes	
16:50-17:10	David Fabian, Patrick Morris and Tibor	ris and Tibor Domingo Gómez-Pérez, Ana I. Gómez and	
	Szabó Francisco-Javier Soto		
	Maximum running times for graph boot-	A Faster Algorithm for the Two Cluster	
	strap percolation processes	Partitioning Problem	
17:10-17:30	Márton Borbényi, Panna Fekete, Aranka Antonio Cañete, Isabel Fernán		
	Hrušková and Ander Lamaison	Alberto Márquez	
	Logarithmic convergence of projective	Conway's fried potato problem: a	
	planes (quadratic) algorithm leading to		
		optimal division for convex polygons	
17:30-17:45	Short break		
17:45-18:45	Guillem Perarnau (Aula 1)	Chair: Anna de Mier	
	Wandering on random digraphs		
18:45-20:45	Welcome reception		

Tuesday, July 5

Time	Aula 1	Aula 2		
9:30-10:30	Marthe Bonamy (Aula 1)	Chair: Lluís Vena		
	One graph to rule them all: forbidden structures and universal graphs			
10:30-11:15	Group picture +	- Coffee break		
	Chair: Guillem PerarnauChair: Marth			
11:15-11:35	Alexander Allin and Alberto Espuny	Leo Liberti, Benedetto Manca and		
	Díaz	Pierre-Louis Poirion		
	An analogue of Chvátal's Hamiltonicity	Random projections for the distance geom-		
	theorem for randomly perturbed graphs	etry problem		
11:35-11:55	Alberto Espuny Díaz and Joseph Hyde	José Manuel Jiménez Cobano, Haydee		
	Powers of Hamilton cycles in graphs per-	Jiménez Tafur and José María Ucha-		
	turbed by a random geometric graph	Enríquez		
		The weighted sum method for multi-		
		objective optimization using Test Sets via		
		Gröbner Bases		
11:55-12:15	Josep Díaz, Öznur Yasar Diner, Maria	Deniz Ağaoğlu Çağırıcı and Onur		
	Serna and Oriol Serra	Çağırıcı		
	On Vertex Bisection Width of Random d-	Unit disk visibility graphs		
	Regular Graphs			
12:15-13:15	Poster session			

List of posters

- Aida Abiad, Jozefien D'haeseleer and **Robin Simoens**. Cospectral generalized Johnson and Grassmann graphs
- Tanbir Ahmed, Luis Boza, María Pastora Revuelta and María Isabel Sanz. Advances on the 3-color off-diagonal generalized Schur numbers $S(3; k_1, k_2, k_3)$
- Gabriela Araujo-Pardo, Cristina Dalfó, Miguel Àngel Fiol and Nacho López. On bipartite biregular Moore graphs
- Lidija Čomić and Paola Magillo. Computation of 2D Discrete Geometric Moments through Inclusion-Exclusion
- Adriana Dapena, Magdalena Lemańska, **María José Souto-Salorio** and Francisco Vazquez-Araujo.

Trees having domination number equal to isolation number

 Magda Dettlaff, Abel Cabrera Martínez, Magdalena Lemańska and Juan Alberto Rodríguez-Velázquez.

Restrained differential of a graph

- Antonio González, **Carmen Hernando** and Mercè Mora. *Distance-equalizer sets of graphs*
- Simon B. Hengeveld and Antonio Mucherino. The discrete side of Distance Geometry: a focus on the 1-dimensional case
- Nacho López, Josep Conde and Gabriela Araujo-Pardo. On local bipartite Moore graphs
- László Németh and László Szalay. Sequences related to square and cube zig-zag shapes

Tuesday, July 5 (cont.)

	Chair: Pascal Schweitzer	Chair: David Orden
15:00-15:20	Béla Bajnok and Péter Pál Pach	Jordi Castellví, Marc Noy and Clément
	On sumsets of nonbases of maximum size	Requilé
		Enumeration of chordal planar graphs and
		maps
15:20-15:40	Anuj Dawar and Danny Vagnozzi	Philippe Nadeau
	A parallel between the descriptive com-	Local parking procedures on the integers
	plexities of finite groups and Latin square	
	graphs	
15:40-16:00	Carlos Marijuán and Miriam Pisonero	Gilad Chase, Neta Dafni, Yuval Filmus
	New Results for the Spectra of Weighted	and Nathan Lindzey
	Graphs of Order 5	Characterizing the Extremal Families in
		Erdős–Ko–Rado Theorems
16:00-16:30	Coffee break	
16:30-17:30	Business meeting	
20:30	Social dinner, Hotel Silken Rio	

Wednesday, July 6

Time	Aula 1	Aula 2		
	Chair: Oriol Serra	Chair: Antonio Macchia		
9:30-9:50	Mario Huicochea	Arnau Padrol, Eva Philippe and Fran-		
	Rainbow solutions of a linear equation with	cisco Santos		
	coefficients in $\mathbb{Z}/p\mathbb{Z}$ - CANCELLED	Many regular triangulations and many		
		polytopes		
9:50-10:10	Daniel Král', Ander Lamaison and Péter	Arnau Padrol, Vincent Pilaud and Ger-		
	Pál Pach	main Poullot		
	Common systems of two equations over the	Deformation cones of graphical zonotopes		
	binary field			
10:10-10:30	Juanjo Rué and Maximilian Wötzel	Bruno Benedetti and Marta Pavelka		
	Normal limiting distributions for systems	2-LC triangulated manifolds are exponen-		
	of linear equations in random sets	tially many		
10:30-11:15	Coffee break			
	<u>Chair:</u> Péter Pál Pach	Chair: José A. Samper		
11:15-11:35	Oriol Serra and Maximilian Wötzel	Michael Joswig, Dante Luber , Georg		
	On a nonabelian Kneser theorem	Loho and Jorge Olarte		
		Generalized Permutahedra and Positive		
		Flag Dressians		
11:35-11:55	Miquel Ortega and Sean Prendiville	Luis Crespo Ruiz and Francisco Santos		
	Extremal Sidon sets are Fourier uniform,	Multitriangulations and tropical Pfaffians		
	with applications to partition regularity			
11:55-12:15	Manuel A. Espinosa-Garcia, Amanda	Julian Pfeifle		
	Montejano, Edgardo Roldán-Pensado and	Fast positive Plücker trees		
	J. David Suárez			
	Sidon-Ramsey and B_h -Ramsey numbers			
12:20-13:20	János Pach (Aula 1)	Chair: Francisco Santos		
	Crossing lemmas for multigraphs?			
13:20	Closure			

Invited talks

Marthe Bonamy (Université de Bordeaux)

One graph to rule them all: forbidden structures and universal graphs

Abstract: Consider all planar graphs on n vertices. What is the smallest graph that contains them all as induced subgraphs?

In this talk, we will gently introduce the audience to the notion of so-called universal graphs (graphs containing all graphs of a given family as induced subgraphs), and focus on the case of graph classes defined by forbidden structures. We present positive and negative results both in dense graphs and in sparse graphs. The audience will also have the answer to the question at the beginning of this abstract, recently established in a breakthrough paper of Dujmović, Esperet, Joret, Gavoille, Micek and Morin.

János Pach (EPFL Lausanne and Rényi Institute Budapest) Crossing lemmas for multigraphs?

Abstract: The celebrated Crossing Lemma of Thurston and Ajtai, Chvátal, Newborn, and Szemerédi gives an asymptotically tight lower bound on the number of edge crossing in any drawing of a graph G in the plane which has n vertices and e > 3n - 6 edges. The lemma has found many applications in topological graph theory, additive number theory, combinatorial geometry, and elsewhere. In order to extend its range of applications, for more than 40 years, there have been many attempts to strengthen this lemma for various special classes of graphs, and to generalize it to multigraphs (where there can be several edges between any pair of vertices). We describe some recent efforts in this direction, and raise several open problems.

Guillem Perarnau (Universitat Politécnica de Catalunya) Wandering on random digraphs

Abstract: Random walks on random graphs is an active area of research with numerous results in the last 20 years. While the theory is well developed for undirected graphs, the directed case is much less understood. Unfortunately, networks that arise in applications are often directed by nature (e.g. World Wide Web, citation network, ...). In recent years, new techniques have been developed to study the directed setting. In this talk I will survey some of the most prominent results in the area, including the study of the random stationary measure and the mixing properties of the chain. Time permitting, I will cover two topics more in-depth. First, I will show how directed edges dramatically increase the time required to visit every vertex of the graph. Second, I will present a mathematical framework for the so-called *'power-law hypothesis'*, a property relating in-degrees with Pagerank – the webpage ranking at the core of Googles search engine.

The results presented are joint work with Xing Shi Cai, Pietro Caputo and Matteo Quattropani.

Pascal Schweitzer (TU Darmstadt)

Symmetry in discrete structures: graphs, groups and algorithms

Abstract: The concept of symmetry is ubiquitous in the study of discrete combinatorial objects. The ensemble of symmetries of an object G is its automorphism group $\operatorname{Aut}(G)$. It provides us with structural information of the object. The group also captures how its symmetries relate to one another. While symmetries are interesting to study in their own right, symmetries also have direct applications in diverse areas that make use of combinatorial objects.

In the talk, I will describe various facets of research surrounding the structure, detection and application of symmetries.

• Regarding the *structure of symmetry*, I will discuss automorphism groups of graphs in minorclosed graph classes. Examples of such graph classes include the class of trees, planar graphs, graphs of bounded genus (i.e., graphs embeddable into a fixed surface without crossings), and graphs of bounded tree width. While a classic result of Frucht shows that every finite group is the automorphism group of a finite graph, Babai showed that with a fixed graph class that excludes a fixed minor not all groups can be represented as automorphism groups. The talk will discuss general structure theorems for the automorphism group of minor-closed graph classes.

- Regarding detection of symmetry, it is well known that the so-called graph isomorphism problem, which asks us to decide whether two given graphs are isomorphic, is universal in the following sense. The computation of the automorphism group of an arbitrary (explicitly given) combinatorial object reduces, in polynomial time, to the graph isomorphism problem. The isomorphism problem in turn reduces to a related problem, the problem of computing a canonical labeling. In some contexts this is referred to as computing a normal form of a given graph. The talk will discuss some recent advances in the research on the theory and implementation of practical graph isomorphism solvers.
- Regarding *application of symmetry*, I will focus on a particular type of application in finite model theory. Specifically, I will touch on the quest for a logic capturing PTIME and discuss how it relates to the graph isomorphism and graph canonization problems.

This talk is in part an overview over various results obtained within the ERC-Project EngageS (https://www.mathematik.tu-darmstadt.de/EngageS) and based on joint work with numerous co-authors.

Places for Lunch

Lunches are self-organised and not included in the registration fee. There are a number of cafeterias in the university area offering a full lunch for about 10 euros. Here are some recommended places near the conference venue. Numbers refer to the map below.

- Cafeterias that offer, sandwiches, platos combinados, and/or mens del da: (1) La Toba, (2) Kiss, (3) Boulevard, (4) Santander Antiguo, (5) La Conchita, (6) Isae, (7) Escudero, (8) Bedoya2.
- Eco-friendly take-away: (9) Ecotierruca.
- More formal/elaborate restaurant with a wider variety of dishes: (10) De Morro Fino.
- The university buildings marked on the map (including the Faculty of Sciences) have cafeterias offering sandwiches and small food.

1 La toba			
. The			
	Engineering	10 De Morro Fino	
Education Graculty of Science	7 Bedoya 2		Hotel Silken Rio
Law Astander Antiglis La Conchita Astander Antiglis La Conchita Isae			

The map also shows the bf Hotel Silken Rio, in El Sardinero, where the social dinner will take place on Tuesday July 5th.